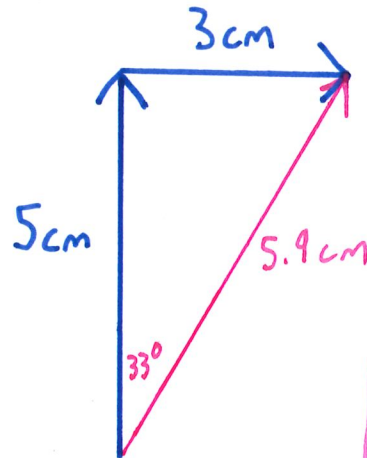


Part 1: Drawing using scale and measurements.

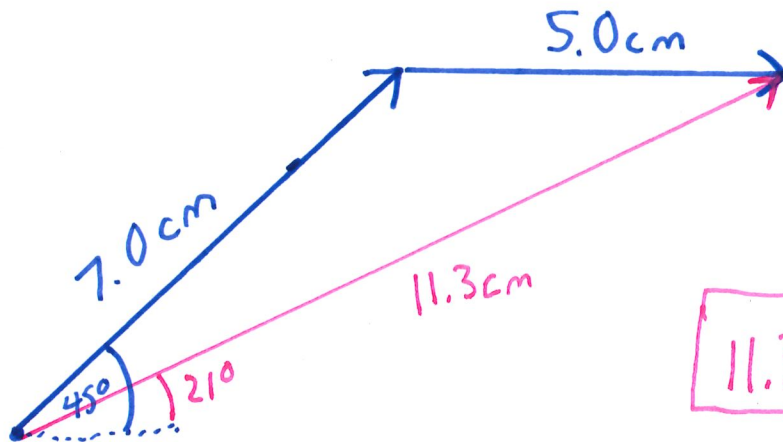
1. Use a ruler and a protractor to draw the following vectors and MEASURE to determine the result of their addition (both magnitude and direction). Give all answers to 2 sig figs.

- a. 5.0 cm North + 3.0 cm East



5.9 cm, 33° East of North

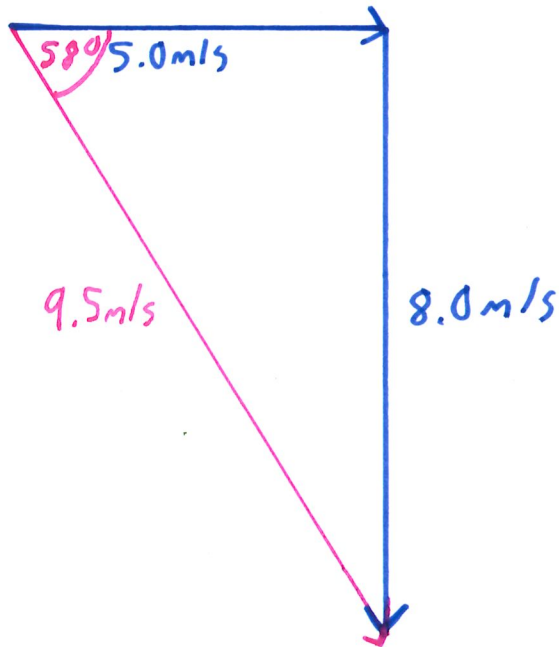
- b. 7.0 cm, 45° North of East + 5.0 cm East



11.3 cm, 21° North of East

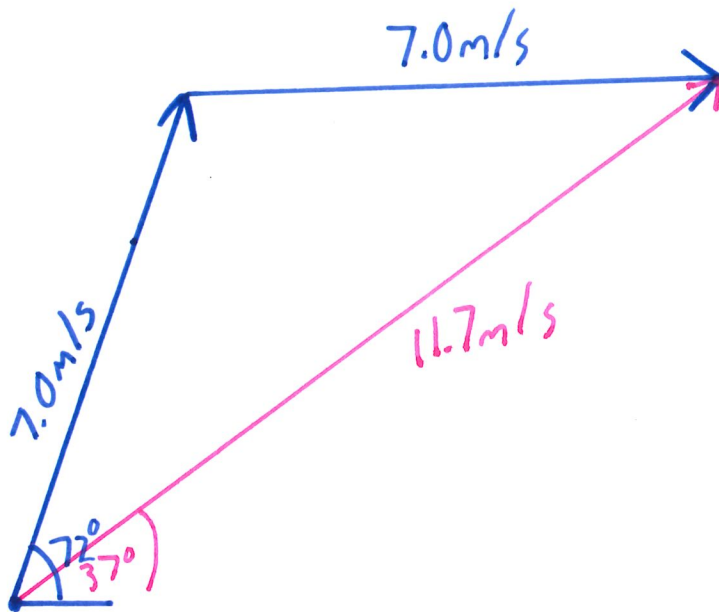
2. Use a scale of $1 \text{ m/s} = 1 \text{ cm}$ to draw and MEASURE to solve each vector addition

a. 5.0 m/s Horizontally + 8.0 m/s Down



9.5 m/s , 58° below
the horizontal

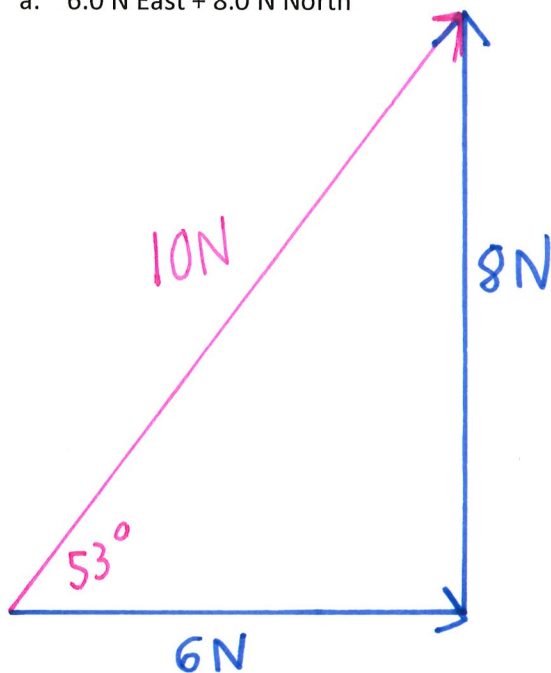
b. 7.0 m/s , 72° above the horizontal + 7.0 m/s horizontally.



11.7 m/s , 37° above
the horizontal

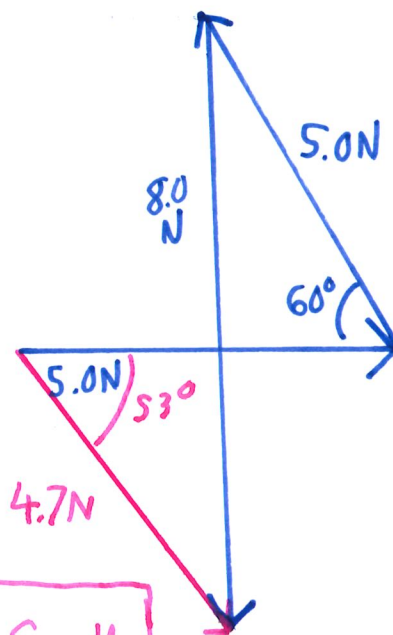
3. Use a scale of 1 N = 1 cm to draw and MEASURE to solve each vector addition

a. 6.0 N East + 8.0 N North



10 N, 53° North of East

b. 5.0 N East + 5.0 N, 60.0° North of West + 8.0 N South



4.7 N, 53° South of East

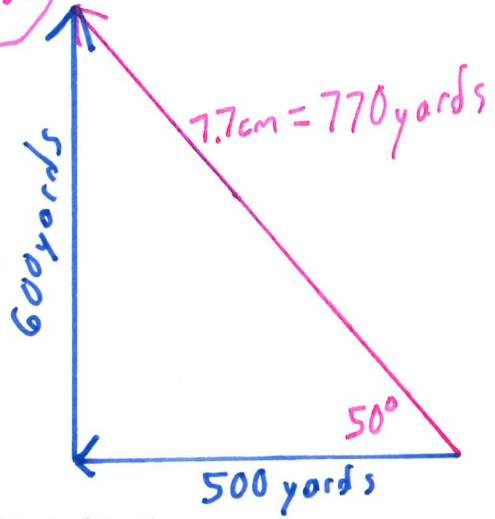
4. Solve each of the following subtractions by drawing scale diagrams:

a. 500 yards West - 600 yards South

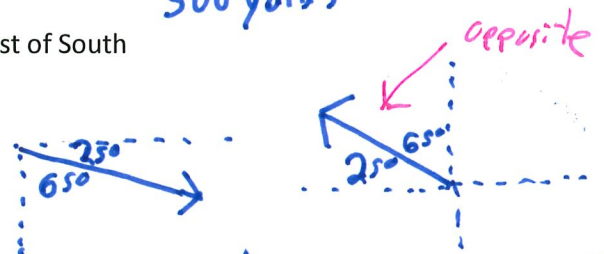
1 cm = 100 yds

500 yards West + 500 yards North

770 yards, 50° North of West



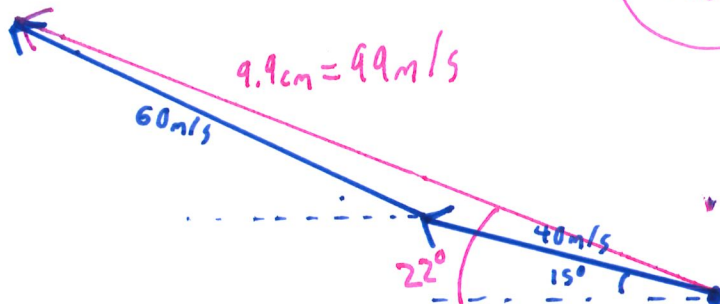
b. 40 m/s, 15° North of West - 60 m/s 65° East of South



40 m/s, 15° North of West + 60 m/s, 25° North of West

1 cm = 10 m/s

99 m/s, 22° North of West



Part 2: Using PhET simulation

Use the link on the Google Classroom, or https://phet.colorado.edu/sims/html/vector-addition/latest/vector-addition_en.html. Then select "Explore 2D"

5.

$ \vec{a} $	18.0	θ	56.3	a_x	10.0	a_y	15.0
-------------	------	----------	------	-------	------	-------	------

What do each of the numbers shown here represent? Fill in with the terms:

Horizontal Component, Vertical Component, Angle, and Magnitude

$|\vec{a}|$ represents *magnitude*

θ represents the *angle*

a_x represents the *x-component of vector*

a_y represents the *y-component of vector*

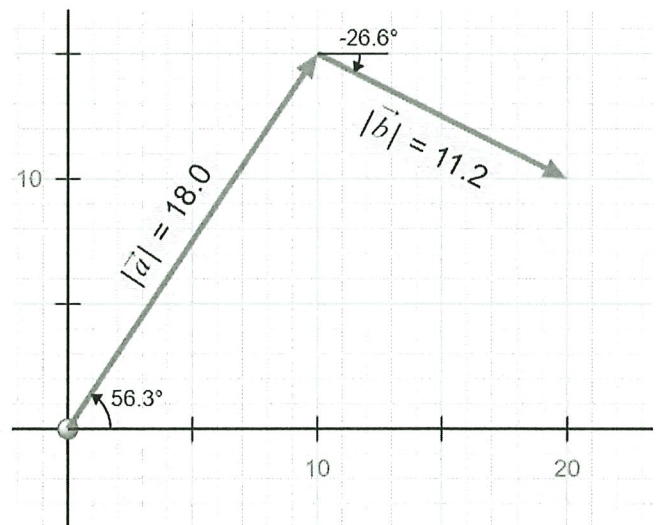
6. What could the following addition of vectors represent:

A: 18.0 m/s, at 56.3° above the horizontal + 11.2 m/s, at 26.6° below the horizontal ✓

B: 18.0 N, at 56.3° North of East + 11.2 N 26.6° South of East ✓

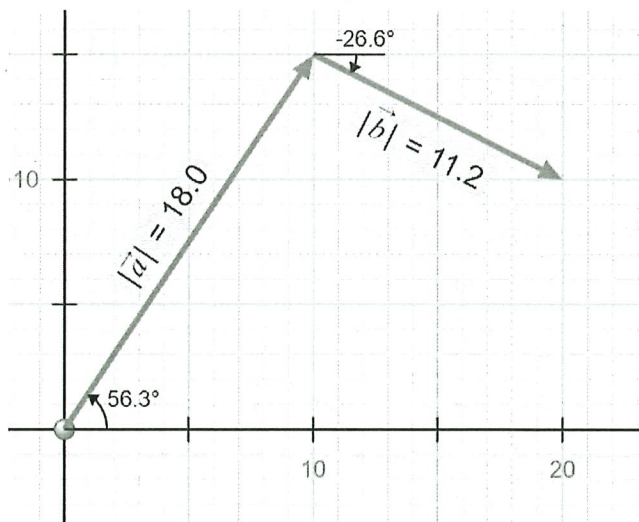
C: 11.2 kilometres, 26.6° down from straight across plus 18.0 kilometres, 56.3° up from straight across.

D: All of the above



7. Draw the two vectors shown and turn on the "Sum", then drag the resultant vector so it connects the start of vector a to the end of vector b . What is the magnitude and direction of the sum?

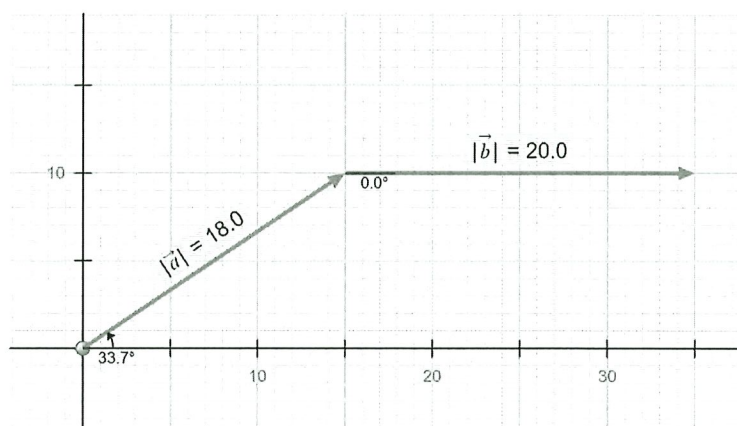
$$\text{mag} = 22.4, 26.6^\circ$$



8. Use the simulation to determine the magnitude and direction of the sum of the vector addition shown:

$$\text{mag} = 36.4$$

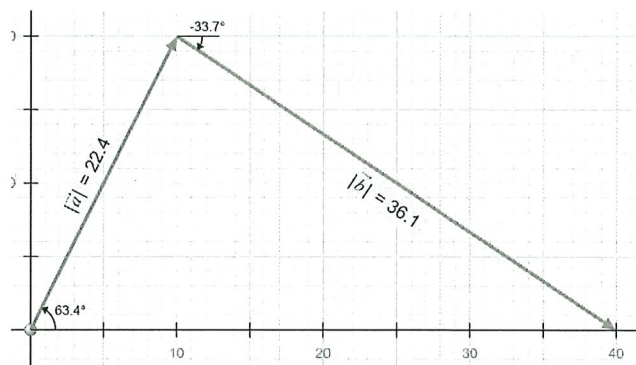
$$\theta = 15.9^\circ$$



9. Use the simulation to determine the magnitude and direction of the sum of the vector addition shown:

$$\text{mag} = 40.0$$

$$\theta = 0^\circ$$



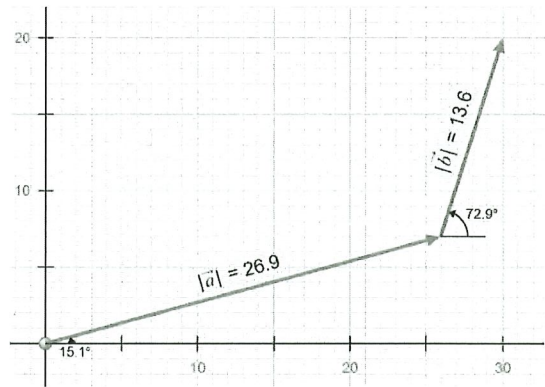
10.

a. What addition is shown in the diagram?

26.9, 15.1° above horizontal
 +
 13.6, 72.9° above horizontal

b. What is the sum of that addition?

36.1, 33.7° above horizontal



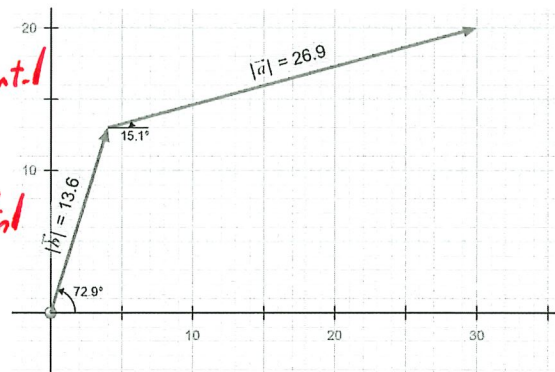
11.

a. What addition is shown in the diagram?

13.6, 72.9° above horizontal
 +
 26.9, 15.1° above horizontal

b. What is the sum of that addition?

36.1, 33.7° above horizontal



c. Does the order of addition matter in vector addition?

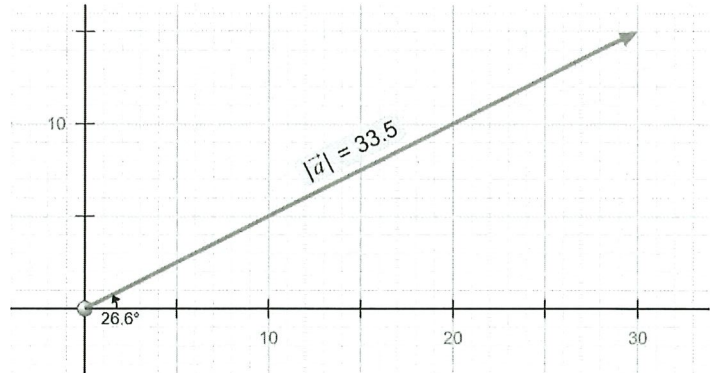
No, answers to 10 b and 11 b
 are the same

12

12. Use the simulation to determine the horizontal and vertical components of the vector shown:

$$a_x = 30.0$$

$$a_y = 15.0$$



13

13. Use the simulation to determine the result of adding 29.2 Newtons at 31° above the horizontal plus 11.2 Newtons at 63.4° above the horizontal. Your answer should have both angle and magnitude.

39.1 N, ~~31.1~~^{39.8}° above the horizontal

39.8°

14

14. Use the simulation to determine the result of adding 18 m/s, 33.7° North of East + 11.2 m/s, 26.6° South of East + 19.0 m/s North.

34.7 m/s, 43.8° North of East

Part 3: Adding and subtracting vectors at right angles using trigonometry.

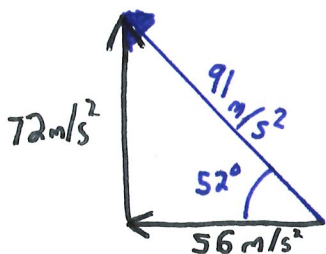
Draw a diagram, and using right angle trigonometry and the Pythagorean theorem to determine the solution to the following:

$$\sin \theta = \frac{\text{Opposite}}{\text{Hypotenuse}}$$

$$\cos \theta = \frac{\text{Adjacent}}{\text{Hypotenuse}}$$

$$\tan \theta = \frac{\text{Opposite}}{\text{Adjacent}}$$

15. 56 m/s^2 West + 72 m/s^2 North.

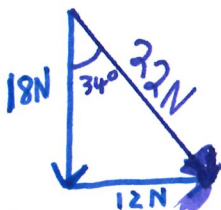


$$\text{Magnitude: } \sqrt{72^2 + 56^2} = 91 \text{ m/s}^2$$

$$\text{Angle: } \tan^{-1}\left(\frac{72}{56}\right) = 52^\circ$$

$91 \text{ m/s}^2, 52^\circ$ North of West

16. 18 newtons South – 12 newtons West
18N South + 12N East

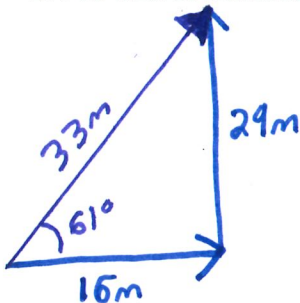


$$\text{Magnitude: } \sqrt{18^2 + 12^2} = 22 \text{ N}$$

$$\text{Angle: } \tan^{-1}\left(\frac{12}{18}\right) = 34^\circ$$

$22 \text{ N}, 34^\circ$ East of South

17. 16 metres horizontally + 29 metres vertically



$$\text{Magnitude: } \sqrt{16^2 + 29^2} = 33 \text{ m}$$

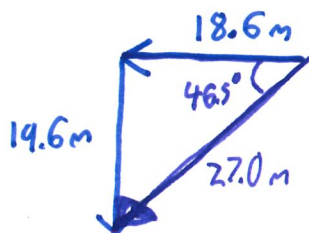
$$\text{Angle: } \tan^{-1}\left(\frac{29}{16}\right) = 61^\circ$$

$33 \text{ m}, 61^\circ$ up from right

18. 6.2 metres West + 19.2 metres South – 12.4 metres East

$$6.2 \text{ m W} - 12.4 \text{ m East} = 6.2 \text{ m W} + 12.4 \text{ m W} = 18.6 \text{ m West}$$

$$18.6 \text{ m West} + 19.2 \text{ m South}$$



$$\text{Magnitude: } \sqrt{19.6^2 + 18.6^2} = 27.0 \text{ m}$$

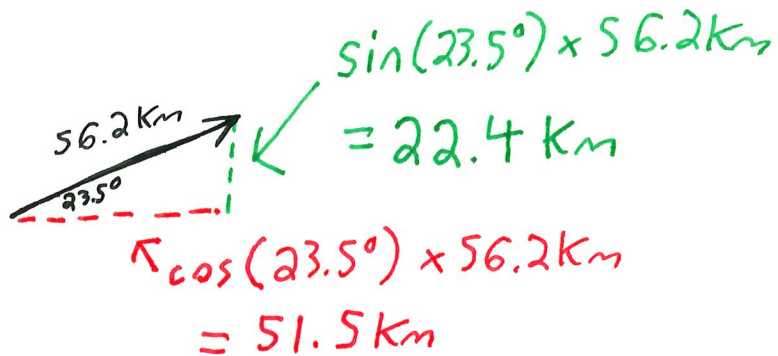
$$\text{Angle: } \tan^{-1}\left(\frac{19.6}{18.6}\right) = 46.5^\circ$$

$27.0 \text{ m}, 46.5^\circ$ South of West

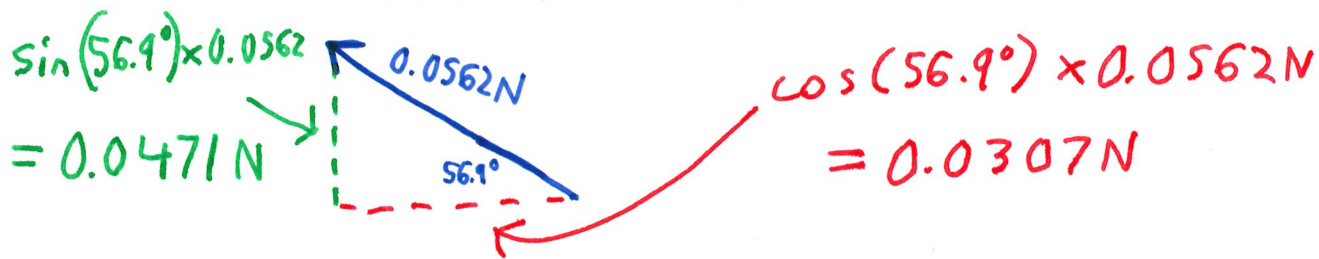
Part 4: Using components to add and subtract vectors

19. Use trigonometry to determine the components of the following vectors:

- a. 56.2 km, at 23.5° above the horizontal



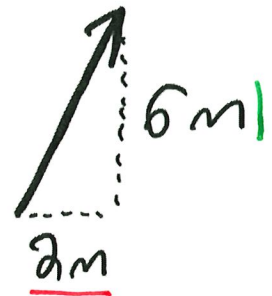
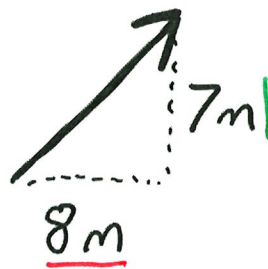
- b. 0.0562 Newtons, at 56.9° North of West



20. Two vectors and their components are shown.

- a. Determine the sum of the horizontal components.

$$8 \text{ m} + 2 \text{ m} = 10 \text{ m}$$



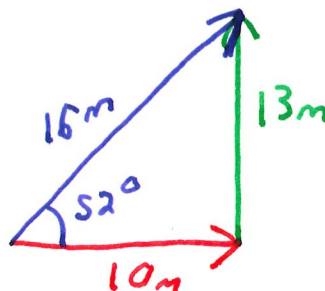
- b. Determine the sum of the
- ^{vertical}
- horizontal components.

$$7 \text{ m} + 6 \text{ m} = 13 \text{ m}$$

- c. Determine result of adding the two vectors, this should be a vector with magnitude and direction.

$$\sqrt{10^2 + 13^2} = 16 \text{ m}$$

$$\tan^{-1}\left(\frac{13 \text{ m}}{10 \text{ m}}\right) = 52^\circ$$

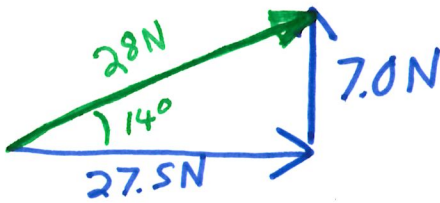
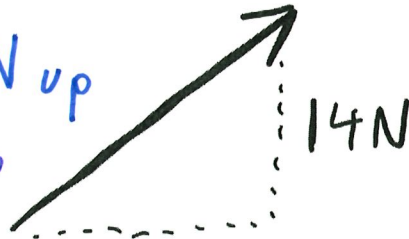
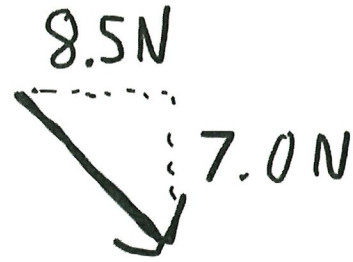


16 m, 52° North of East

21. Determine the result of adding the two vectors shown.

Horizontal components : $8.5\text{N} + 19\text{N} = 27.5\text{N}$

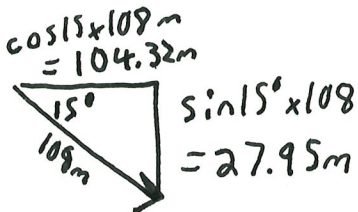
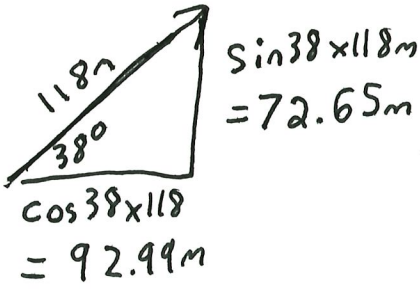
Vertical components : $-7.0\text{N} + 14\text{N} = 7.0\text{N up}$
 ↑ since it is going down



$\tan^{-1}\left(\frac{7.0\text{N}}{27.5\text{N}}\right) = 14^\circ$
 $19\text{N} \sqrt{27.5^2 + 7.0^2} = 28\text{N}$

28N, 14° above horizontal

22. Determine the components for each of the following vectors, and then use the components to determine the resultant vector.

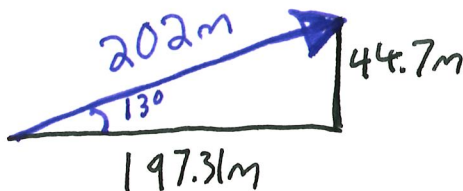


Horizontal components
 $92.99\text{m} + 104.32\text{m} = 197.31\text{m}$

Vertical components
 $72.65\text{m} - 27.95\text{m} = 44.7\text{m}$

$\sqrt{197.31^2 + 44.7^2} = 202\text{m}$

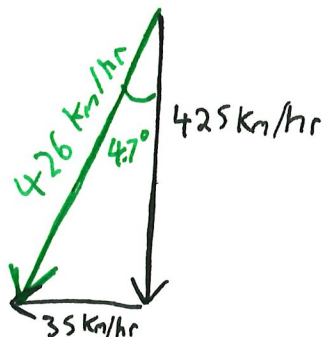
$\tan^{-1}\left(\frac{44.7\text{m}}{197.31\text{m}}\right) = 13^\circ$



202m, 13° above horizontal

Part 5: Solving Problems

23. A plane is flying due South. A 35 km/hr wind blows due West. The plane flies with a velocity of 425 km/hr. What is the actual speed and direction the plane is flying?



$$\tan^{-1}\left(\frac{35}{425}\right) = 4.7^\circ$$

$$\sqrt{425^2 + 35^2}$$

$$= 426 \text{ km/hr}$$

426 km/hr, 4.7° West of South

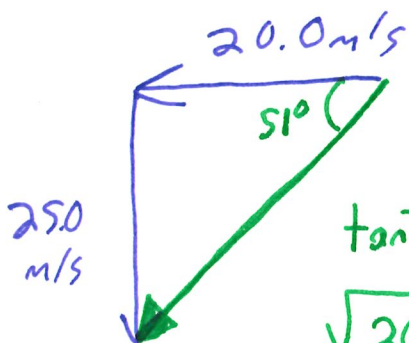
24. What is the acceleration of a car that turns from travelling 25.0 m/s North to travelling 20.0 m/s West?

$$a = \frac{\Delta v}{t} = \frac{v_f - v_i}{t}$$

$$v_f = 20.0 \text{ m/s West}$$

$$v_i = 25.0 \text{ m/s North}$$

$$v_f - v_i \rightarrow 20.0 \text{ m/s West} - 25 \text{ m/s North} \\ = 20.0 \text{ m/s West} + 25 \text{ m/s South}$$



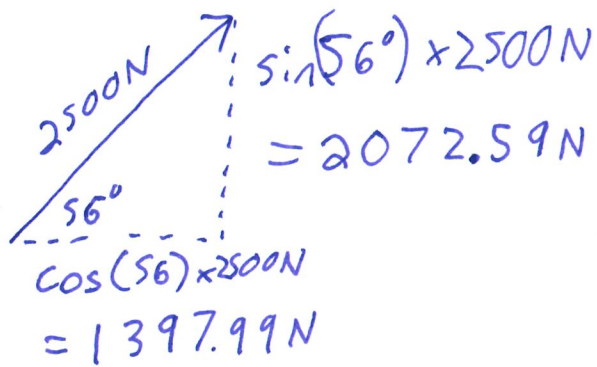
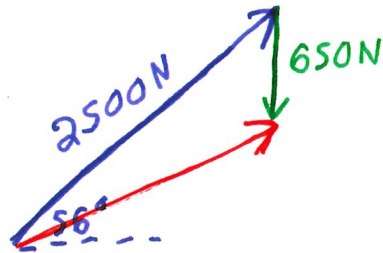
$$\tan^{-1}\left(\frac{25}{20}\right) = 51^\circ$$

$$\sqrt{20^2 + 25^2} = 32.0 \text{ m/s}$$

$$a = \frac{v_f - v_i}{t} = \frac{32.0 \text{ m/s}, 51^\circ \text{ South of West}}{3.0 \text{ sec}}$$

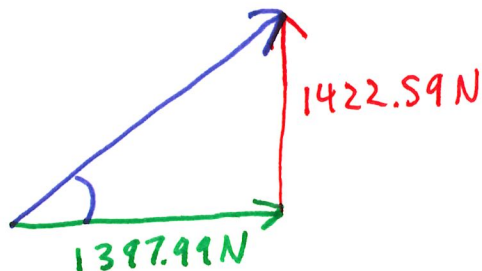
$$= 10.7 \frac{\text{m}}{\text{s}^2}, 51^\circ \text{ South of West}$$

25. A rocket is pointed at an angle of 56° above the horizontal and the engines output 2500 N of force, gravity pulls the rocket straight downwards with a force of 650 N. What is the net force acting on the rocket?



Total horizontal force
is 1397.99 N

Total vertical force
 $2072.59 N - 650 N$
= 1422.59 N



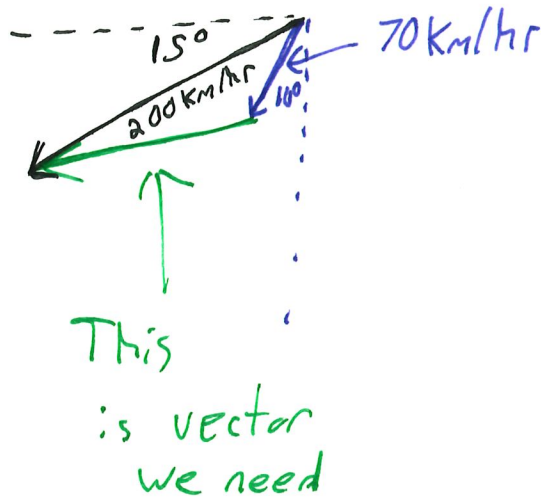
$$\sqrt{1397.99^2 N + 1422.59^2 N} = 1994.53 N$$

$$\tan^{-1}\left(\frac{1422.59 N}{1397.99 N}\right) = 45^\circ$$

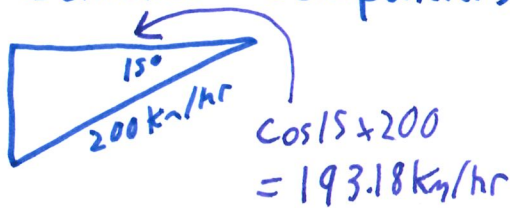
$2.0 \times 10^3 N, 45^\circ$ above horizontal

26. A pilot wishes to reach a city 400.0 km away in a direction of 15° S of W in two hours. If there is a wind of 70 km/h blowing at 10° W of S. What must be the heading and air speed of the plane?

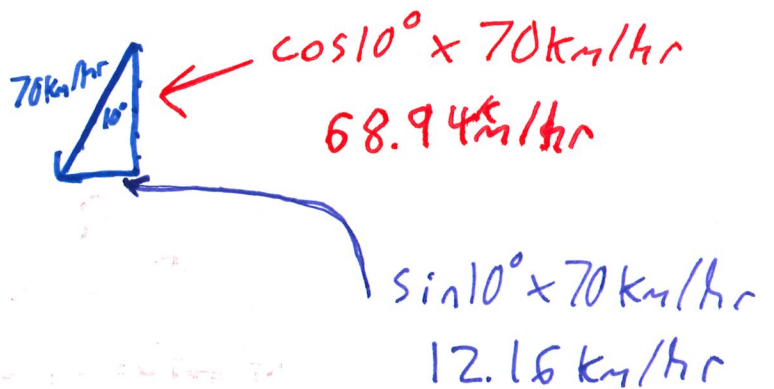
Resultant velocity must be $\frac{400.0 \text{ km}}{2 \text{ hrs}} = 200 \text{ km/hr}$, 15° S of W



Consider Components:



$\sin 15^\circ = \frac{\text{Opp}}{200}$
 $\text{Opp} = 51.76 \text{ km/hr}$



We know $68.94 \text{ km/hr} + v_y = 51.76 \text{ km/hr}$ $v_y = 17.18 \text{ km/hr North}$
 and $12.16 \text{ km/hr} + v_x = 193.18 \text{ km/hr}$ $v_x = 181.02 \text{ km/hr West}$

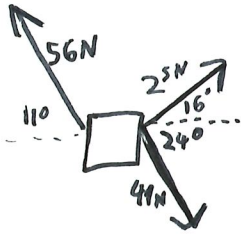


$\sqrt{181.02^2 + 17.18^2} = 182 \text{ km/hr}$
 $\tan^{-1}\left(\frac{17.18}{181.02}\right) = 5.4^\circ$

182 km/hr, 5.4° North of West

27. Three forces act on a 5.0 kg block. There is a 25 N force at 16° North of East, a 49 N force at 34° South of East and a 56 N force acting at 11° North of West.

a. What is the net force acting on the block?



$$\cos 11^\circ \times 56 = -54.97 \text{ N}$$

$$\sin 11^\circ \times 56 = 10.69 \text{ N}$$



$$\cos 16^\circ \times 25 = 24.03 \text{ N}$$

$$\sin 16^\circ \times 25 = 6.89 \text{ N}$$



$$\cos 34^\circ \times 49 \text{ N} = 40.62 \text{ N}$$

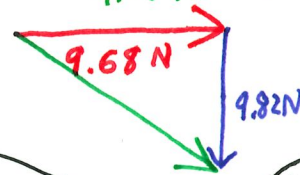
$$\sin 34^\circ \times 49 \text{ N} = -27.4 \text{ N}$$

Total vertical
 $10.69 \text{ N} + 6.89 \text{ N} - 27.4 \text{ N} = -9.82 \text{ N}$
 9.82 N down

Total horizontal
 $-54.97 \text{ N} + 24.03 \text{ N} + 40.62 \text{ N} = 9.68 \text{ N East}$

$$\sqrt{9.68^2 + 9.82^2} = 13.79$$

$$\tan^{-1}\left(\frac{9.82}{9.68}\right) = 45^\circ$$



14 N, 45° South of East

b. What is the acceleration of the block ($F_{net} = ma$)

$$a = \frac{F_{net}}{m} = \frac{13.79 \text{ N, } 45^\circ \text{ South of East}}{5.0 \text{ kg}} = 2.758 \text{ m/s}^2, 45^\circ \text{ South of East}$$

c. What will be the displacement of the block after travelling for 5.0 seconds?

$$d = v_0 t + \frac{1}{2} a t^2 \rightarrow d = 34.475 \text{ m, } 45^\circ \text{ South of East}$$

d. What will be the kinetic energy of the block after it has been travelling for 5.0 seconds?

$$v_f = v_0 + a t \rightarrow v_f = 13.79 \text{ m/s}$$

$$E_k = \frac{1}{2} m v^2 = 475 \text{ J}$$